

Chapter 2: Solving Linear Inequalities

2.1 Writing and Graphing Inequalities

What is an inequality?

Example 1: Writing Inequalities

Write each sentence as an inequality

- a) A number w minus 3.5 is less than or equal to -2
- b) Three is less than a number n plus 5
- c) Zero is greater than or equal to twice a number x plus 1

Example 2: Checking Solutions

Tell whether -4 is a solution of each inequality

- a) $x + 8 < -3$
- b) $-4.5x > -21$

Example 3: Graphing Inequalities

Graph each inequality

- a) $y \leq -3$
- b) $2 < x$
- c) $x > 0$

Try on your own: Graph the inequality

7. $b > -8$

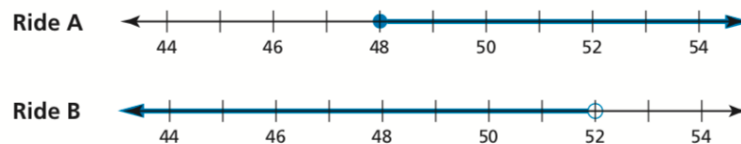
8. $1.4 \geq g$

9. $r < \frac{1}{2}$

10. $v \geq \sqrt{36}$

Example 4: Writing Inequalities from Graphs

The graphs below show the height restrictions of two rides at six flags. Write an inequality that represents the height restrictions that represents the height restrictions.



Homework:

5-12, 15-23odd, 41-46, 57

2.1 Exercises

Dynamic Solutions available at BigIdeasMath.com

Vocabulary and Core Concept Check

- COMPLETE THE SENTENCE** A mathematical sentence using the symbols $<$, $>$, \leq , or \geq is called a(n)_____.
- VOCABULARY** Is 5 in the solution set of $x + 3 > 8$? Explain.
- ATTENDING TO PRECISION** Describe how to graph an inequality.
- DIFFERENT WORDS, SAME QUESTION** Which is different? Write “both” inequalities.

w is greater than or equal to -7 .

w is no less than -7 .

w is no more than -7 .

w is at least -7 .

Monitoring Progress and Modeling with Mathematics

In Exercises 5–12, write the sentence as an inequality.
(See Example 1.)

- A number x is greater than 3.
- A number n plus 7 is less than or equal to 9.
- Fifteen is no more than a number t divided by 5.
- Three times a number w is less than 18.
- One-half of a number y is more than 22.
- Three is less than the sum of a number s and 4.
- Thirteen is at least the difference of a number v and 1.
- Four is no less than the quotient of a number x and 2.1.

13. MODELING WITH MATHEMATICS

On a fishing trip, you catch two fish. The weight of the first fish is shown. The second fish weighs at least 0.5 pound more than the first fish. Write an inequality that represents the possible weights of the second fish.



- 14. MODELING WITH MATHEMATICS** There are 430 people in a wave pool. Write an inequality that represents how many more people can enter the pool.

HOURS

Monday–Friday: 10 A.M. – 6 P.M.

Saturday–Sunday: 10 A.M. – 7 P.M.


Maximum Capacity: 600


In Exercises 15–24, tell whether the value is a solution of the inequality. (See Example 2.)

- $r + 4 > 8; r = 2$
- $5 - x < 8; x = -3$
- $3s \leq 19; s = -6$
- $17 \geq 2y; y = 7$
- $-1 > \frac{x}{2}; x = 3$
- $\frac{4}{z} \geq 3; z = 2$
- $14 \geq -2n + 4; n = -5$
- $-5 \div (2s) < -1; s = 10$
- $20 \leq \frac{10}{2z} + 20; z = 5$
- $\frac{3m}{6} - 2 > 3; m = 8$
- MODELING WITH MATHEMATICS** The tallest person who ever lived was approximately 8 feet 11 inches tall.
 - Write an inequality that represents the heights of every other person who has ever lived.
 - Is 9 feet a solution of the inequality? Explain.

26. **DRAWING CONCLUSIONS** The winner of a weight-lifting competition bench-pressed 400 pounds. The other competitors all bench-pressed at least 23 pounds less.
- Write an inequality that represents the weights that the other competitors bench-pressed.
 - Was one of the other competitors able to bench-press 379 pounds? Explain.

ERROR ANALYSIS In Exercises 27 and 28, describe and correct the error in determining whether 8 is in the solution set of the inequality.

27. 
$$\begin{aligned} -y + 7 &< -4 \\ -8 + 7 &< -4 \\ -1 &< -4 \end{aligned}$$
 8 is in the solution set.

28. 
$$\begin{aligned} \frac{1}{2}x + 2 &\leq 6 \\ \frac{1}{2}(8) + 2 &\leq 6 \\ 4 + 2 &\leq 6 \\ 6 &\leq 6 \end{aligned}$$
 8 is not in the solution set.

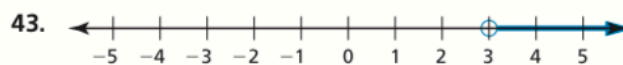
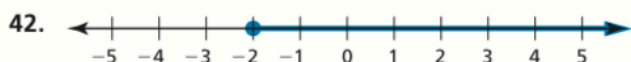
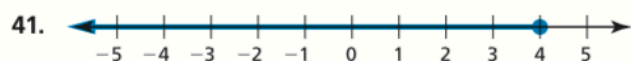
In Exercises 29–36, graph the inequality. (See Example 3.)

- $x \geq 2$
- $z \leq 5$
- $-1 > t$
- $-2 < w$
- $v \leq -4$
- $s < 1$
- $\frac{1}{4} < p$
- $r \geq -|5|$

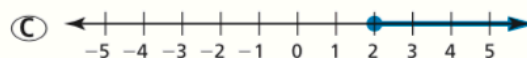
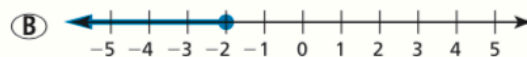
In Exercises 37–40, write and graph an inequality for the given solution set.

- $\{x \mid x < 7\}$
- $\{n \mid n \geq -2\}$
- $\{z \mid 1.3 \leq z\}$
- $\{w \mid 5.2 > w\}$




In Exercises 41–44, write an inequality that represents the graph. (See Example 4.)



45. **ANALYZING RELATIONSHIPS** The water temperature of a swimming pool must be no less than 76°F . The temperature is currently 74°F . Which graph correctly shows how much the temperature needs to increase? Explain your reasoning.



46. **MODELING WITH MATHEMATICS** According to a state law for vehicles traveling on state roads, the maximum total weight of a vehicle and its contents depends on the number of axles on the vehicle. For each type of vehicle, write and graph an inequality that represents the possible total weights w (in pounds) of the vehicle and its contents.

Maximum Total Weights		
		
2 axles, 40,000 lb	3 axles, 60,000 lb	4 axles, 80,000 lb

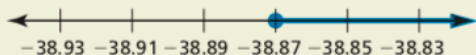
47. **PROBLEM SOLVING** The Xianren Bridge is located in Guangxi Province, China. This arch is the world's longest natural arch, with a length of 400 feet. Write and graph an inequality that represents the lengths ℓ (in inches) of all other natural arches.



48. **THOUGHT PROVOKING** A student works no more than 25 hours each week at a part-time job. Write an inequality that represents how many hours the student can work each day.

49. **WRITING** Describe a real-life situation modeled by the inequality $23 + x \leq 31$.

50. **HOW DO YOU SEE IT?** The graph represents the known melting points of all metallic elements (in degrees Celsius).



- a. Write an inequality represented by the graph.
b. Is it possible for a metallic element to have a melting point of -38.87°C ? Explain.
51. **DRAWING CONCLUSIONS** A one-way ride on a subway costs \$0.90. A monthly pass costs \$24. Write an inequality that represents how many one-way rides you can buy before it is cheaper to buy the monthly pass. Is it cheaper to pay the one-way fare for 25 rides? Explain.

Subway Prices	
One-way ride	\$0.90
Monthly pass	\$24.00

52. **MAKING AN ARGUMENT** The inequality $x \leq 1324$ represents the weights (in pounds) of all mako sharks ever caught using a rod and reel. Your friend says this means no one using a rod and reel has ever caught a mako shark that weighs 1324 pounds. Your cousin says this means someone using a rod and reel *has* caught a mako shark that weighs 1324 pounds. Who is correct? Explain your reasoning.

53. **CRITICAL THINKING** Describe a real-life situation that can be modeled by more than one inequality.

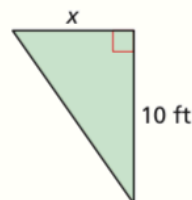
54. **MODELING WITH MATHEMATICS** In 1997, Superman's cape from the 1978 movie *Superman* was sold at an auction. The winning bid was \$17,000. Write and graph an inequality that represents the amounts all the losing bids.

MATHEMATICAL CONNECTIONS In Exercises 55–58, write an inequality that represents the missing dimension x .

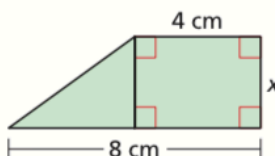
55. The area is less than 42 square meters.



56. The area is greater than or equal to 8 square feet.



57. The area is less than 18 square centimeters.



58. The area is greater than 12 square inches.



59. **WRITING** A runner finishes a 200-meter dash in 35 seconds. Let r represent any speed (in meters per second) faster than the runner's speed.

- a. Write an inequality that represents r . Then graph the inequality.
b. Every point on the graph represents a speed faster than the runner's speed. Do you think every point could represent the speed of a runner? Explain.

Maintaining Mathematical Proficiency

Reviewing what you learned in previous grades and lessons

Solve the equation. Check your solution. (Section 1.1)

60. $x + 2 = 3$

61. $y - 9 = 5$

62. $6 = 4 + y$

63. $-12 = y - 11$

Solve the literal equation for x . (Section 1.5)

64. $v = x \cdot y \cdot z$

65. $s = 2r + 3x$

66. $w = 5 + 3(x - 1)$

67. $n = \frac{2x + 1}{2}$