

2.2 Solving Inequalities Using Addition or Subtraction

Spiral Review:

Solve for x

$$y = 5x - 8 + 4xy$$

Example 1: Solving an Inequality Using Addition

Solve the inequality. Graph the solution.

$$x - 6 \geq -10$$

Example 2: Solving an Inequality Using Subtraction

Solve each inequality. Graph the solution

a) $x + 8 \leq 5$

b) $-8 < 1.4 + m$

Try on your own: Solve the inequality. Graph the solution.

$$\frac{5}{6} \leq y + \frac{1}{3}$$

Example 3: Modeling with Mathematics

During the summer a window unit air conditioner uses 1,100 watts of electricity. The circuit will over load at 1,800 watts.

a) Write and solve an inequality that represents the wattage you can add without overloading.

b) Which of the following can be on with the air conditioner?

Appliance	Watts
Clock radio	50
Blender	300
Hot plate	1200
Toaster	800

Homework: 16, 20, 24, 25, 31, 36*, 38*

Vocabulary and Core Concept Check

- VOCABULARY** Why is the inequality $x \leq 6$ equivalent to the inequality $x - 5 \leq 6 - 5$?
- WRITING** Compare solving equations using addition with solving inequalities using addition.

Monitoring Progress and Modeling with Mathematics

In Exercises 3–6, tell which number you would add to or subtract from each side of the inequality to solve it.

3. $k + 11 < -3$

4. $v - 2 > 14$

5. $-1 \geq b - 9$

6. $-6 \leq 17 + p$

In Exercises 7–20, solve the inequality. Graph the solution. (See Examples 1 and 2.)

7. $x - 4 < -5$

8. $1 \leq s - 8$

9. $6 \geq m - 1$

10. $c - 12 > -4$

11. $r + 4 < 5$

12. $-8 \leq 8 + y$

13. $9 + w > 7$

14. $15 \geq q + 3$

15. $h - (-2) \geq 10$

16. $-6 > t - (-13)$

17. $j + 9 - 3 < 8$

18. $1 - 12 + y \geq -5$

19. $10 \geq 3p - 2p - 7$

20. $18 - 5z + 6z > 3 + 6$

In Exercises 21–24, write the sentence as an inequality. Then solve the inequality.

21. A number plus 8 is greater than 11.

22. A number minus 3 is at least -5 .

23. The difference of a number and 9 is fewer than 4.

24. Six is less than or equal to the sum of a number and 15.

25. **MODELING WITH MATHEMATICS** You are riding a train. Your carry-on bag can weigh no more than 50 pounds. Your bag weighs 38 pounds. (See Example 3.)

a. Write and solve an inequality that represents how much weight you can add to your bag.

b. Can you add both a 9-pound laptop and a 5-pound pair of boots to your bag without going over the weight limit? Explain.

26. **MODELING WITH MATHEMATICS** You order the hardcover book shown from a website that offers free shipping on orders of \$25 or more. Write and solve an inequality that represents how much more you must spend to get free shipping.



Price: \$19.76

ERROR ANALYSIS In Exercises 27 and 28, describe and correct the error in solving the inequality or graphing the solution.

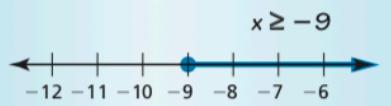
27. 

$$\begin{aligned}
 & -17 < x - 14 \\
 & -17 + 14 < x - 14 + 14 \\
 & -3 < x
 \end{aligned}$$



28. 

$$\begin{aligned}
 & -10 + x \geq -9 \\
 & -10 + 10 + x \geq -9 \\
 & x \geq -9
 \end{aligned}$$



29. **PROBLEM SOLVING** An NHL hockey player has 59 goals so far in a season. What are the possible numbers of additional goals the player can score to match or break the NHL record of 92 goals in a season?

30. MAKING AN ARGUMENT In an aerial ski competition, you perform two acrobatic ski jumps. The scores on the two jumps are then added together.

Ski jump	Competitor's score	Your score
1	117.1	119.5
2	119.8	

a. Describe the score that you must earn on your second jump to beat your competitor.

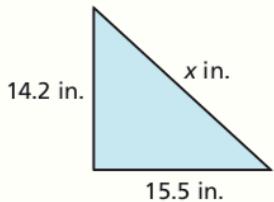
b. Your coach says that you will beat your competitor if you score 118.4 points. A teammate says that you only need 117.5 points. Who is correct? Explain.

31. REASONING Which of the following inequalities are equivalent to the inequality $x - b < 3$, where b is a constant? Justify your answer.

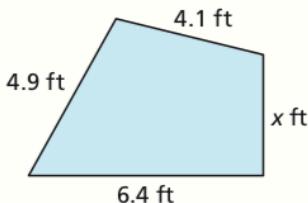
(A) $x - b - 3 < 0$ (B) $0 > b - x + 3$
 (C) $x < 3 - b$ (D) $-3 < b - x$

MATHEMATICAL CONNECTIONS In Exercises 32 and 33, write and solve an inequality to find the possible values of x .

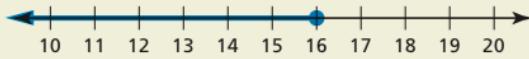
32. Perimeter < 51.3 inches



33. Perimeter ≤ 18.7 feet

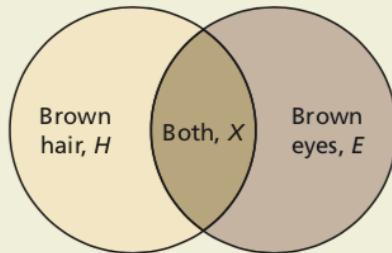


34. THOUGHT PROVOKING Write an inequality that has the solution shown in the graph. Describe a real-life situation that can be modeled by the inequality.



35. WRITING Is it possible to check all the numbers in the solution set of an inequality? When you solve the inequality $x - 11 \geq -3$, which numbers can you check to verify your solution? Explain your reasoning.

36. HOW DO YOU SEE IT? The diagram represents the numbers of students in a school with brown eyes, brown hair, or both.



Determine whether each inequality must be true. Explain your reasoning.

a. $H \geq E$ b. $H + 10 \geq E$
 c. $H \geq X$ d. $H + 10 \geq X$
 e. $H > X$ f. $H + 10 > X$

37. REASONING Write and graph an inequality that represents the numbers that are *not* solutions of each inequality.

a. $x + 8 < 14$
 b. $x - 12 \geq 5.7$

38. PROBLEM SOLVING Use the inequalities $c - 3 \geq d$, $b + 4 < a + 1$, and $a - 2 \leq d - 7$ to order a , b , c , and d from least to greatest.

Maintaining Mathematical Proficiency

Reviewing what you learned in previous grades and lessons

Find the product or quotient. (*Skills Review Handbook*)

39. $7 \cdot (-9)$ 40. $-11 \cdot (-12)$ 41. $-27 \div (-3)$ 42. $20 \div (-5)$

Solve the equation. Check your solution. (*Section 1.1*)

43. $6x = 24$ 44. $-3y = -18$ 45. $\frac{s}{-8} = 13$ 46. $\frac{n}{4} = -7.3$